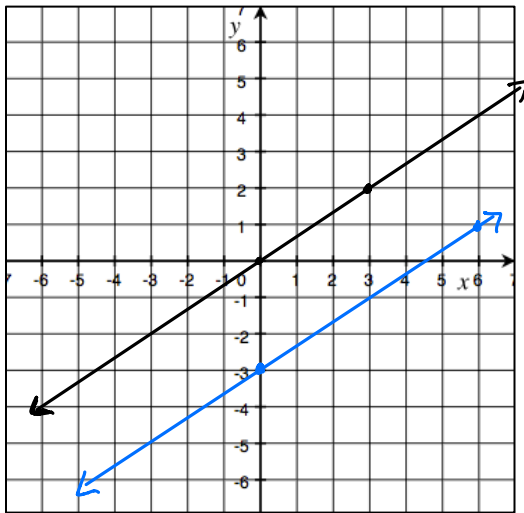


LEARNING OBJECTIVE: We will look at systems of equations that have no solutions and systems that have infinitely many solutions. (G8M4L23)

CONCEPT DEVELOPMENT:

Graph the following system of equations in the space provided:

$$\begin{cases} y = \frac{2}{3}x \\ y = \frac{4}{6}x - 3 \end{cases}$$

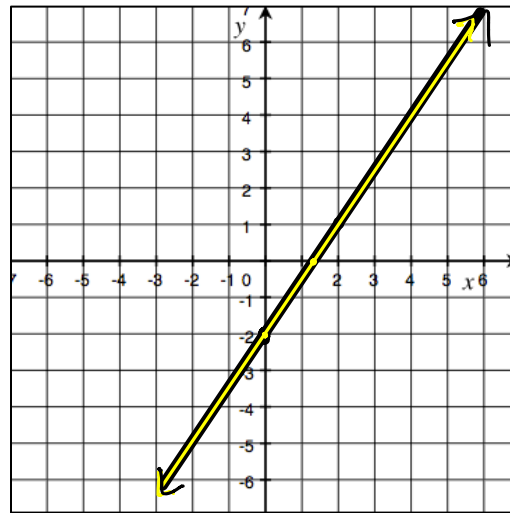


- Lines are parallel
- Lines have the same slope.
- Different y -intercepts

Parallel lines will have no points of intersection. THE SYSTEM OF EQUATIONS HAS NO SOLUTION!!!!!!

Graph the following system of equations in the space provided:

$$\begin{cases} y = \frac{3}{2}x - 2 \\ 3x - 2y = 4 \end{cases}$$



- Two lines are the same. They are collinear.
- Same slope.
- Same y -intercept

Lines that have the same slope and same y -intercept form a system with INFINITELY MANY SOLUTIONS!!!!

GUIDED PRACTICE:**Steps for Determining the Number of Solutions to a System of Linear Equations**

1. Identify the slope of each linear equation.
2. If the slopes are the same, identify the y-intercept.
- 3a. If the y-intercepts are the same, the two equations represent the same line and there are **INFINITELY MANY SOLUTIONS**.
- 3b. If the y-intercepts are different, the two equations are distinct parallel lines and have **NO SOLUTION**.
- 3c. If the slopes are different, there will be **ONE UNIQUE SOLUTION**.

For each problem below, determine if the system has infinitely many solutions, no solution, or one unique solution.

$\begin{cases} 6x - 2y = 5 \\ 4x - 3y = 5 \end{cases}$ $\begin{aligned} 6x - 2y &= 5 \\ -2y &= -6x + 5 \\ y &= 3x - \frac{5}{2} \end{aligned}$ $\begin{aligned} 4x - 3y &= 5 \\ -3y &= -4x + 5 \\ \frac{-3y}{-3} &= \frac{-4x + 5}{-3} \\ y &= \frac{4}{3}x - \frac{5}{3} \end{aligned}$ <p style="font-size: 2em; margin-top: 10px;"># of Solutions? 1</p>	$\begin{cases} 7x + 2y = -4 \\ x - y = 5 \end{cases}$ $\begin{aligned} 7x + 2y &= -4 \\ 2y &= -7x - 4 \\ \frac{2y}{2} &= \frac{-7x - 4}{2} \\ y &= -\frac{7}{2}x - 2 \end{aligned}$ $\begin{aligned} x - y &= 5 \\ -y &= -x + 5 \\ y &= x - 5 \end{aligned}$ <p style="font-size: 2em; margin-top: 10px;"># of Solutions? 1</p>
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Not the same slope!!
1 Solution!

NAME: _____

Math _____, Period _____

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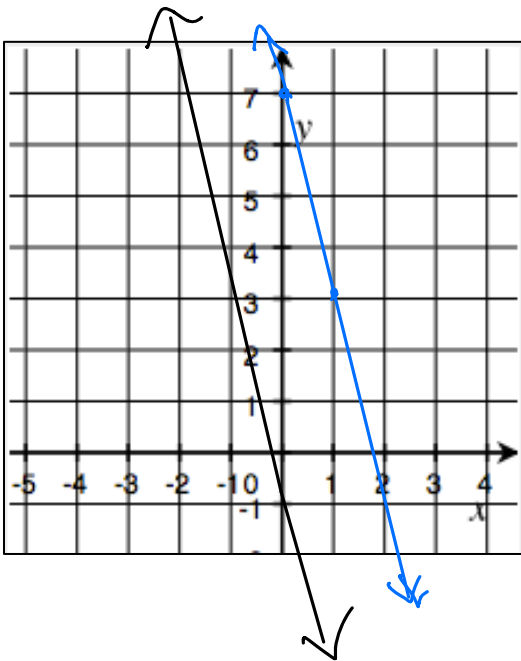
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$$\begin{cases} 12x + 3y = -2 \\ 4x + y = 7 \end{cases}$$

$$y = -4x - \frac{2}{3} \quad y = 4x + 7$$

$$Ax + By = C$$

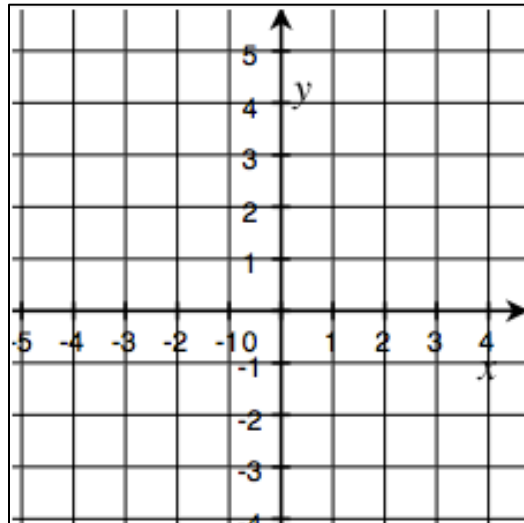
$$y = -\frac{A}{B}x + \frac{C}{B}$$



of Solutions? 0

? Same slope
? different y-int.

$$\begin{cases} -2x + 8y = 14 \\ x = 4y + 1 \end{cases}$$



of Solutions?

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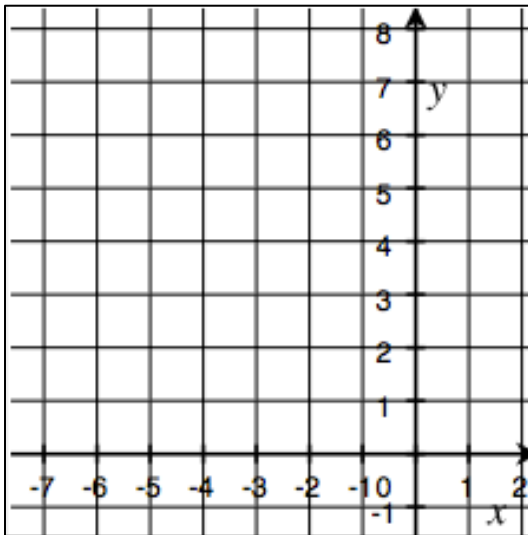
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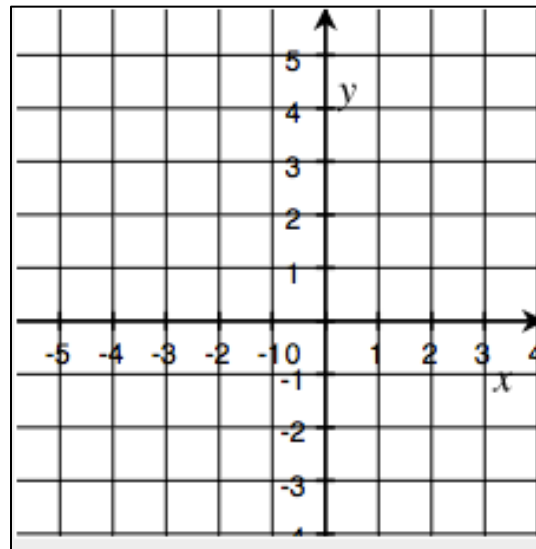
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$$\begin{cases} 5y = \frac{15}{4}x + 25 \\ y = \frac{3}{4}x + 5 \end{cases}$$

$$\begin{cases} 9x + 6y = 3 \\ 3x + 2y = 1 \end{cases}$$



of Solutions?



of Solutions?

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INDEPENDENT PRACTICE:

For each problem below, determine if the system has infinitely many solutions, no solution, or one unique solution.

$$\begin{cases} y = x - 3 \\ 2x - 2y = 6 \end{cases}$$

$$\begin{cases} y = -\frac{3}{2}x + 4 \\ 3x + 2y = 8 \end{cases}$$

$$\begin{cases} y = \frac{3}{5}x - 3 \\ y = \frac{3}{5}x + 1 \end{cases}$$

$$\begin{cases} y = \frac{3}{2}x \\ 3x - 2y = -5 \end{cases}$$

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$$\begin{cases} 3y = 5x - 15 \\ 3y = 13x - 2 \end{cases}$$

$$\begin{cases} 3x - 5y = 0 \\ y = \frac{3}{5}x \end{cases}$$

$$\begin{cases} 10x + 4y = -23 \\ y = -\frac{5}{2}x + 23 \end{cases}$$

$$\begin{cases} y = x + 1 \\ x - y = 1 \end{cases}$$

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ACTIVATING PRIOR KNOWLEDGE:

We can identify the number of solutions in equations in one variable.

$5x + 45 = 2(x + 18) + 3x$	$3x - 4 = 4x - (x + 4)$
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CLOSURE:

Write a system of equations that has no solutions and be ready to explain why you know it has no solutions.

TEACHER NOTES:

Lesson 26 from ENY Mod 4, Grade 8. And first half of Lesson 27...

HW: Khan Graphing Systems of Equations (goes with lesson 50, but it's fine to assign this now)

Khan: Graphing Systems with one, zero, or infinite solutions