

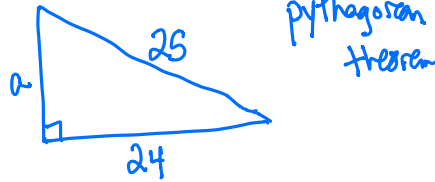
LEARNING OBJECTIVE: We will rearrange formulas and solve for variables.
(Alg1M1L14)

ACTIVATING PRIOR KNOWLEDGE:

We know how to use formulas to find unknown quantities.

* The side of one leg of a right triangle is 24 inches, and the hypotenuse is 25 inches. What is the length of the other leg?

DRAW A PICTURE



$$a^2 + 24^2 = 25^2$$

$$a^2 + 576 = 625$$

$$\sqrt{a^2} = \sqrt{149} \quad a = 7$$

The average of 3 numbers is 67. One number is 45, and another is 71. What is the third number?

$$3 \left(\frac{45 + 71 + x}{3} \right) = (67) 3$$

$$45 + 71 + x = 201$$

$$116 + x = 201$$

$$-116 \quad -116$$

$$\boxed{x = 85}$$

CONCEPT DEVELOPMENT:

We can use properties of equality and inverse operations to rearrange formulas, and solve for specific variables.

Example: $A = \pi r^2$ Let's solve for r .

FORMULA FOR
AREA OF A CIRCLE!

$$\begin{aligned} A &= \pi r^2 \\ \frac{A}{\pi} &= \frac{\pi r^2}{\pi} \\ \sqrt{\frac{A}{\pi}} &= \sqrt{r^2} \\ r &= \sqrt{\frac{A}{\pi}} \end{aligned}$$

GUIDED PRACTICE:**Steps for Solving For Variables**

1. Study the particular formula and identify the variable you are trying to solve for.
2. Perform inverse operations and use properties of equality to isolate the appropriate variable.

The formula for the perimeter of a rectangle is $P = 2(l + w)$. Solve for w .

$$\begin{aligned} \frac{P}{2} &= \frac{2(l+w)}{2} & P &= 2(l+w) \\ \frac{P}{2} &= l+w & P &= 2l+2w \\ -l &-l & -2l &-2l \\ \frac{P}{2} - l &= w & \frac{P-2l}{2} &= \frac{2w}{2} \\ \frac{P}{2} - l &= w & \frac{P-2l}{2} &= w \end{aligned}$$

The formula for volume of a sphere is $V = \frac{4}{3}\pi r^3$. Solve for the radius.

$$\begin{aligned} \frac{3}{4}(V) &= \left(\frac{4}{3}\pi r^3\right) \frac{3}{4} \\ \frac{3V}{4} &= \frac{\pi r^3}{\pi} \\ \sqrt[3]{\frac{3V}{4\pi}} &= \sqrt[3]{r^3} \\ r &= \sqrt[3]{\frac{3V}{4\pi}} \end{aligned}$$

The surface area of a cone is $S = \pi r^2 + \pi r l$. Solve for l .

$$\begin{aligned} S &= \pi r^2 + \pi r l \\ S - \pi r^2 &= \pi r l \\ \frac{S - \pi r^2}{\pi r} &= \frac{\pi r l}{\pi r} \\ \frac{S - \pi r^2}{\pi r} &= l \\ \frac{S}{\pi r} - r &= l \end{aligned}$$

The formula $E = \frac{1}{2} k x^2$ is used to find the potential energy E of a spring with spring constant k that has been stretched by length x . Solve the formula for x .

$$\begin{aligned} 2(E) &= \left(\frac{1}{2} k x^2\right) 2 \\ \frac{2E}{k} &= \frac{k x^2}{k} \\ \sqrt{\frac{2E}{k}} &= \sqrt{x^2} \\ \sqrt{\frac{2E}{k}} &= x \end{aligned}$$

<p>The formula for the average of three numbers is $A = \frac{x+y+z}{3}$. Solve for z.</p> $3(A) = \left(\frac{x+y+z}{3}\right) 3$ $3A = x+y+z$ $\begin{array}{r} -x-y \\ -x-y \end{array}$ <div style="border: 1px solid black; padding: 5px; width: fit-content;"> $3A - x - y = z$ </div>	<p>The formula for Fahrenheit is $F = 32 + \frac{9}{5}C$. Solve for Celsius.</p> $F = 32 + \frac{9}{5}C$ $\begin{array}{r} -32 \quad -32 \\ \frac{5}{9}(F-32) = \left(\frac{9}{5}C\right) \frac{5}{9} \end{array}$ $\frac{5}{9}F - \frac{160}{9} = C$
<p>Solve for y.</p> $\frac{y-b}{m} = x.$ $\frac{y-b}{m} \times \frac{m}{1} \quad \text{CROSS MULTIPLY!}$ $y-b = mx$ $\begin{array}{r} +b \quad +b \end{array}$ <div style="border: 1px solid black; border-radius: 15px; padding: 5px; width: fit-content;"> $y = mx + b$ </div> <p style="text-align: center;">SLOPE-INTERCEPT FORM</p>	<p>Solve for q.</p> $\frac{m}{n} = \frac{p}{q}$ $\frac{mq}{n} = \frac{np}{m}$ <div style="border: 1px solid black; padding: 5px; width: fit-content;"> $q = \frac{np}{m}$ </div>
<p>Solve for m.</p> $km = \frac{m}{2} + p.$ <p style="text-align: right;">NO GO!</p> $km = \frac{m}{2} + p$ $\begin{array}{r} -\frac{m}{2} \quad -\frac{m}{2} \end{array}$ $km - \frac{m}{2} = p$ <p style="text-align: right;">FACTOR OUT "m"</p> $m\left(\frac{k-\frac{1}{2}}{2}\right) = p$ $\frac{m}{2\left(k-\frac{1}{2}\right)} = \frac{p}{k-\frac{1}{2}}$ <div style="border: 1px solid black; padding: 5px; width: fit-content;"> $m = \frac{2p}{k-\frac{1}{2}}$ </div>	<p>Solve for s.</p> $rs - t = us + v$ $\begin{array}{r} -us \quad -us \end{array}$ <p style="text-align: right;">get all "s" on same side.</p> $rs - us - t = v$ $\begin{array}{r} +t \quad +t \end{array}$ $rs - us = v + t$ <p style="text-align: right;">FACTOR OUT "s"</p> $\frac{s(r-u)}{r-u} = \frac{v+t}{r-u}$ <div style="border: 1px solid black; padding: 5px; width: fit-content;"> $s = \frac{v+t}{r-u}$ </div>

INDEPENDENT PRACTICE:

Solve for the variable.

Simple Interest is calculated as $I = Prt$.
Solve for t .

$$\frac{I}{Pr} = \frac{Prt}{Pr}$$

$$t = \frac{I}{Pr}$$

The standard form for the equation of a line is $Ax + By = C$. Solve for y .

$$Ax + By = C$$

$$-Ax \quad -Ax$$

$$\frac{By}{B} = \frac{C - Ax}{B}$$

$$y = \frac{C - Ax}{B}$$

 $g\left(h + \frac{2}{3}\right) = 1$.
Solve for h .

$$\frac{g\left(h + \frac{2}{3}\right)}{g} = \frac{1}{g}$$

$$h + \frac{2}{3} = \frac{1}{g}$$

$$h = \frac{1}{g} - \frac{2}{3}$$

 $a(n - 3) + 8 = bn$.
Solve for n .

$$a(n - 3) + 8 = bn$$

$$an - 3a + 8 = bn$$

$$+3a - 8 \quad +3a - 8$$

$$an = bn + 3a - 8$$

$$-bn \quad -bn$$

$$an - bn = 3a - 8$$

$$\frac{n(a - b)}{a - b} = \frac{3a - 8}{a - b}$$

$$n = \frac{3a - 8}{a - b}$$

 $x = \frac{1 + a}{1 - a}$.
Solve for a .

$$\frac{x}{1} = \frac{1 + a}{1 - a}$$

$$x(1 - a) = 1 + a$$

$$x - xa = 1 + a$$

$$+xa \quad +xa$$

$$x = 1 + a + xa$$

$$-1 \quad -1$$

$$x - 1 = a + xa$$

$$\frac{x - 1}{x + 1} = \frac{a(x + 1)}{x + 1}$$

$$a = \frac{x - 1}{x + 1}$$

 $a^2 + b^2 = c^2$.
Solve for b .

$$a^2 + b^2 = c^2$$

$$-a^2 \quad -a^2$$

$$b^2 = c^2 - a^2$$

$$\sqrt{b^2} = \sqrt{c^2 - a^2}$$

$$b = \sqrt{c^2 - a^2}$$

