

**LEARNING OBJECTIVE:** We will solve equations with variable expressions in the denominator and rewrite equations as compound equations. (Alg1M1L13)

**ACTIVATING PRIOR KNOWLEDGE:**

We can solve equations with variables in the denominator.

$\frac{7}{3x+9} = \frac{1}{8}$ $3x+9 = 56$ $\begin{array}{r} -9 \quad 9 \\ \hline \frac{3x}{3} = \frac{47}{3} \end{array}$ <div style="border: 1px solid black; padding: 5px; display: inline-block; margin-left: 20px;"> <math>x = \frac{47}{3}</math> </div>	$\frac{6}{7x+5} = \frac{1}{9}$ $7x+5 = 54$ $\begin{array}{r} -5 \quad -5 \\ \hline \frac{7x}{7} = \frac{49}{7} \end{array}$ <div style="border: 1px solid black; padding: 5px; display: inline-block; margin-left: 20px;"> <math>x = 7</math> </div>
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**CONCEPT DEVELOPMENT:**

We should rewrite expressions as compound statements noting any values for the variables that are disallowed.

Examples:

$\frac{5}{x+2}$  has a meaningful value for all values of  $x$ , except  $x = -2$ .

Why? Because  $\frac{5}{0}$  would be dividing by zero, and we do not want to do that!

So,  $\frac{5}{x+2}$  should be read as a compound statement:

$$\frac{3x-6}{x-2} = \frac{3(x-2)}{x-2} \quad \frac{5}{x+2} \text{ and } x+2 \neq 0$$

What is the value of  $\frac{3x-6}{x-2}$ ? What values of  $x$  are disallowed?

$$x \neq 2$$

What are the values of  $x$  that are **not** permissible in this expression?

$\frac{10}{x+5} \quad x \neq -5$	$\frac{x^2 - 25}{(x^2 - 9)(x + 4)}$ $\frac{(x-3)(x+3)}{(x-3)(x+3)}$ $x \neq 3, x \neq -4, x \neq -3$
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**GUIDED PRACTICE:****Steps to Solving Equations with Variable Expressions in the Denominator**

1. Rewrite the Equation as a System of Equations.
2. Solve the equation and exclude the values of x that lead a denominator of 0.
3. Express your solution in set notation.

$\frac{1}{x} = \frac{3}{x-2} \text{ and } x \neq 0$ $\text{and } x \neq 2$ $3x = x - 2 \quad \{-1\}$ $\begin{array}{r} -x \\ -x \end{array}$ $\frac{2x}{2} = \frac{-2}{2} \quad \boxed{x = -1}$	$\frac{2}{x} = \frac{3}{x-4} \text{ and } x \neq 0 \quad *$ $\text{and } x \neq 4$ $3x = 2x - 8 \quad \{-8\}$ $\begin{array}{r} -2x \\ -2x \end{array}$ $\boxed{x = -8}$
$\frac{x+3}{x-2} = \frac{5}{x-2} \text{ and } x \neq 2$ $5(x-2) = (x+3)(x-2)$ $5(x-2) - (x+3)(x-2) = 0$ $(x-2)(5-x-3) = 0 \quad -x+2=0 \text{ or } x-2=0$ $\textcircled{(x-2)} \textcircled{(x-2)} = 0 \text{ (1)}$ $\frac{(x-2)(x-2)}{x-2} = 0$ $x = 2$ $\emptyset \{ \}$	$\frac{x}{x+6} = \frac{6}{x+6} \text{ and } x \neq -6$ $x = -6$ $\{ \} \emptyset$
$\frac{x}{7-x} = \frac{2x}{7} \text{ and } x \neq 7$ $2x(7-x) = x$ $14x - 2x^2 = x$ $\begin{array}{r} -x \\ -x \end{array} \quad \{0, 6.5\}$ $13x - 2x^2 = 0$ $x(13-2x) = 0$ $x = 0 \quad 13-2x = 0$	$\frac{3+x}{3-x} = \frac{3+2x}{3-2x} \text{ and } x \neq 3$ $\text{and } x \neq 1.5$ $(3-x)(3+2x) = (3+x)(3-2x)$ $9+6x-3x-2x^2 = 9+3x-6x-2x^2$ $3x = -3x$ $\frac{6x}{6} = \frac{0}{6}$ $\boxed{x = 0}$ $\{0\}$

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**INDEPENDENT PRACTICE:**

Problem Set from Lesson 18?

**CLOSURE:**

Write an equation that will have the restriction  $x \neq -3$ ,  $x \neq 14$ , and  $x \neq 0$ .

**NOTES:**

This maps to Lesson 18 in Alg 1 Mod 1 of ENY.